Graph-based Semi-Supervised Learning by Strengthening Local Label Consistency

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ABSTRACT

Graph-based algorithms have drawn much attention thanks to their impressive success in semi-supervised setups. For better model performance, previous studies have learned to transform the topology of the input graph. However, these works only focus on optimizing the original nodes and edges, leaving the direction of augmenting existing data insufficiently explored. In this paper, we propose a novel heuristic pre-processing technique, namely Local Label Consistency Strengthening (L2CS), which automatically expands new nodes and edges to refine the label consistency within a dense subgraph. Our framework can effectively benefit downstream models by substantially enlarging the original training set with high-quality generated labeled data and refining the original graph topology. To justify the generality and practicality of L2CS, we couple it with the popular graph convolution network and graph attention network to perform extensive evaluations on three standard datasets. In all setups tested, our method boosts the average accuracy by a large margin of 4.7% and consistently outperforms the state-of-the-art.

CCS CONCEPTS

- Mathematics of computing → Mathematics of computing
- Computing methodologies → Supervised learning by classification

KEYWORDS

semi-supervised learning, topology enhanced transformation, node classification

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1 INTRODUCTION

Numerous real-world data can be represented as graphs, e.g., social networks [15, 18], citation networks [12, 19, 29], protein network [7], and knowledge graphs [13, 22]. In many cases, large-scale annotated data is expensive to obtain. The so-called graph-based Semi-Supervised Learning (SSL), which holds promise to bootstrap applications even with limited supervision, has therefore attracted increasing research interest. Different from the traditional sample independent scenarios, graph-based SSL models tend to mine the structural relational information to boost effectiveness. Correspondingly, some existing methods have shown that optimizing the input graph structure is beneficial [23, 28]. However, generative ways to refine the topology and the information propagation along the edges are unexplored. In this paper, we propose to mitigate these limitations by a new strategy which strengthens local label consistency, thereby improving the model performance.

Specifically, earlier works develop the classical regularization methods, which achieve SSL by smoothing features or model predictions over local neighborhoods using explicit regularization schemes [2, 17]. Although this direction has been well studied, a later thread of algorithms, namely graph convolution networks, has demonstrated state-of-the-art performance and drawn much attention [3, 11, 25]. By utilizing flexible aggregation strategies, these models selectively fuse the local features of a graph into the hidden representations of its target nodes. To further perform downstream tasks, the hidden layers are coupled with specific task layers [11, 25]. One common characteristic of these two lines of models is that they both adopt the presence of smoothness in the graph structure as a basic assumption. Recently, to better exploit
annotated resources, researchers propose to modify the topology of the input graph [1, 20, 28]. However, to our knowledge, all such methods are limited within handling the existing graph topology.

Inspired by the discussion on the relationship between information similarity within the same community and information propagation [14, 28], we explore a novel research direction for the first time, namely Local Label Consistency Strengthening (L²CS). Through generating some key high-quality nodes and edges, L²CS improves the label consistency of the set of nodes that are structurally closely related to guide more properly feature smoothing on the graph. Specifically, L²CS first identifies dense subgraphs through overlapping clustering algorithms. For each subgraph, by jointly considering node attributes and edge links, it generates a new node with high-quality attributes and a corresponding low-entropy label predicted via the local labeled original nodes in the given data. Lastly, L²CS connects generated nodes with their corresponding original nodes to facilitate information propagation, yielding an updated graph. In addition, we find that this simple pre-processing technique also enhances the class separability of node attributes. Therefore, by producing a high-quality augmented training set, L²CS generally further renders the performance of subsequent SSL models stronger.

To validate the practical usefulness of L²CS, we perform extensive evaluations on the SSL benchmark with three standard datasets. Coupled with two popular models (i.e., Graph Convolutional Network (GCN) and Graph Attention Network (GAT)), our method This is the first study which expands the original graph topology of the ultimate objectives of our algorithm boils to: compared with empirically validated by the experiments of [14, 28]. Therefore, one given the observed presence of graph node communities, has been theoretically closely related to guide more properly feature smoothing along the edges. (3) In the extensive evaluations of SSL on three standard datasets, our method significantly boosts two popular base algorithms and substantially sets new state-of-the-art scores.

2 OUR APPROACH

By implying the widely-adopted assumption of existing graph-based SSL models, i.e., features exhibit smoothness along the graph edges [14, 24, 26, 27], Yang et al. [28] propose a criterion to assess training samples and given graph, which is highly correlated to the subsequent modeling performance: Criterion 6: The higher the label consistency in the subgraph, the better the propagation of feature along the edges. This criterion, which is intuitively evident given the observed presence of graph node communities, has been empirically validated by the experiments of [14, 28]. Therefore, one of the ultimate objectives of our algorithm boils to: compared with the original graph G, the augmented data should satisfy Criterion 6 equally well, or even better.

As illustrated in Figure 1, to achieve this goal, in the first step, we learn to partition the original graph into different dense subgraphs (i.e., clusters) based on graph structure. Next, for each cluster, we automatically generate a new node, whose attributes can be regarded as the multiple sampling results on attributes of existing original nodes in the same dense subgraph. Considering the fact that multiple sampling of distribution can stabilize its posterior probability (i.e., Law of Large Numbers), compared with original nodes, generated nodes naturally have better class separability in terms of attributes. Consequently, while labels of some generated nodes can be directly confirmed from the original nodes, the labels of remaining generated nodes can also be roughly determined even with a very simple classifier. Lastly, since most edges between generated nodes and their corresponding original nodes can maintain label consistency, the updated graph G′ is deemed to have high quality (cf. Criterion 6) and has a much larger volume than the original G, thus effectively benefiting subsequent algorithms.

2.1 Substructure-based Overlapping Clustering

In real-world scenarios, it is quite common that a node belongs to multiple communities (dense subgraphs), e.g., an author publishes a highly impacted paper on machine learning theory, which may get cited by different communities such as computer vision and natural language processing. Therefore, we identify subgraphs through overlapping clustering, which is a well-studied topic in community detection. Its workflow of overlapping clustering is two-phased. First, it learns to cluster nodes within local regions. To handle nodes belonging to multiple neighborhoods, it will create personas for each cluster. Next, it performs a standard global clustering and re-associates the persons whose sources are the same. We denote the resulting set of dense subgraphs as S′.

2.2 Refinement based on Label Consistency

From the generative perspective of graph [16], original nodes in a cluster Cm ∈ S′ become |Cm| samples from the golden distribution of attributes. Similarly, the attributes of the corresponding generated node x ⊤ ∈ X ⊤ can be generated through multiple samplings, i.e., aggregating the attributes of original nodes as

\[ x(i) = \frac{\sum_{j \in Cm} x(j)}{|Cm|}, x(j) \in X. \]

where X ⊤ denotes the attribute matrix of all generated nodes, and Y ⊤ is for the label matrix, likewise. To determine the values of Y ⊤, we proceed with our discussions case by case.

"Winner takes all": We assume that the nodes in the same dense subgraph share similar features/label. Hence, for each generated node, if its original nodes are from the training set, i.e., have annotated labels, then it can straightforward inherit the dominating (i.e., most numerous) label, such that

\[ y(i) = [0, \ldots, 0, 1, \ldots, 0], \quad n_j = \max(n_0, \ldots, n_k), \]

where np (p = 0, · · · , k) is the occurrence of the p-th kind of label observed in Cm. Y ⊤ denotes the label matrix of this category of generated nodes. In practice, we find applying the additional constraint of n ≥ 2 can guarantee the reliability of assigned labels. Data Augmentation. However, only a small portion (e.g., roughly 1/3 in the Cora dataset) of generated nodes can be directly labeled using Eq. (2). For other generated nodes, we find that the label propagation paradigm leads to unsatisfactory results, mainly due to two reasons: on the one hand, real-world graphs (e.g., Cora, Citeseer, and Pubmed) are often not fully connected, so many nodes cannot receive the broadcast of training labels; on the other hand, long-range dependencies may lead to under-smoothing. As theoretically explained by [9], the stability of Eq. (1) will get strengthened if
the number of samplings increases, and $X^r$ will thereafter exhibit stronger class separability (of attributes). This property inspires us to attempt a novel self-learning scheme to handle unlabeled generated nodes. To begin with, we learn a simple binary classifier based on the already-labeled generated nodes (i.e., the union of generated nodes labeled in the last paragraph and those labeled in the previous iterations). Next, after predicting on-the-fly labels using this classifier, we filter out the generated nodes whose labels are assigned with probability lower than a given “labeling threshold”. The above two steps are iteratively performed to produce enough generated nodes with high-quality predicted labels.

2.3 Downstream Coupling

By merging high-quality labeled generated nodes into $G$ (i.e., inserting generated nodes and connecting them with original nodes in the corresponding cluster), we obtain the updated graph $G' = \{V', E', X', Y'\}$ as shown in Figure 1. Apart from the significantly enlarged volume, another outstanding advantage of $G'$ is that, for each dense graph, as generated node becomes the common neighbor of all its original nodes (i.e., they are linked with new edges), the maximum distance between any two nodes in the same dense subgraph becomes 2, i.e., long-range dependencies get generally shortened. Finally, $G'$ can be fed into subsequent graph-based SSL models, with the single aggregation operation for $v_i$ at depth $l$ being represented as $h_i^l = \sigma(\sum_{j \in \mathcal{V}_l \setminus \{n\}} a_{ij} W h_j^{l-1})$ ($h_i^l$ is the hidden representation of $v_i$ at the $l$-th layer, $\mathcal{V}_l$ is the neighbor set of $v_i$, $W$ is a learnable linear transformation matrix, $\sigma(\cdot)$ is an element-wise nonlinear activation function, and $a_{i,j}$ is the evaluation parameter set in feature aggregation, e.g., the attention function of GAT).

3 EXPERIMENTS

Following previous studies [11, 25, 29], we demonstrate the effectiveness of $L^2CS$ on the widely-adopted semi-supervised node classification benchmark.

3.1 Experimental Setup

Datasets. Our evaluation is based on three datasets (i.e., Cora, Citeseer, and Pubmed [29]) which are the de facto standards for assessing graph-based SSL algorithms. They are all sampled via citation networks, where nodes are for research publications and edges for the citation. In Cora and Citeseer, node attributes are represented as bag-of-words, while Pubmed uses TF-IDF weights. For a fair comparison, we adopt the same splits as Yang et al. [29], i.e., 20 training samples per class, 500/1000 verification/test samples.

Baselines. To justify the generality of $L^2CS$, we respectively integrate it with GCN [11] and GAT [25] as they are the two most popular graph-based SSL methods in the GNN community. As shown in Table 1, we select three recently-published approaches as our reference baselines [10, 27, 30]. In addition, we include six variants of GCN [3, 4, 6, 16, 27, 28, 32], and three variants of GAT [6, 16, 24, 31].

Parameters. In practice, we find that our proposed $L^2CS$ is robust towards configuration variations. Therefore, we exploit the default setting for parameters without much fine-tuning. To be specific, for overlapping clustering we select the Ego-Splitting algorithm [5, 21], with the resolution set at 1.0. In the high-level information diffusion step, we utilize the simple GBDT [8] as our classifier, with a learning rate at 0.25, max depth at 3, and other parameters selected as default. During all experiments, we terminate the training when the verification accuracy no longer increases for 2K iterations. Test scores based on the models and hyper-parameters with the best verification performance are reported, and all the hyper-parameters used are listed (the number of iterative diffusions and the labeling threshold is 10 and 0.99, respectively).

3.2 Results Analysis

Table 1 reports the results of our baseline methods, base algorithms (GCN and GAT), and $L^2CS$-enhanced models ($L^2CS$-GCN and $L^2CS$-GAT). To reduce randomness, we run each model for 10 independent trials and calculate the average score and standard deviation. On all the three datasets, $L^2CS$-GAT consistently sets new state-of-the-art performance, with margins of 0.6% to 3.3% compared with the best baselines which are not coupled with $L^2CS$. Before being stacked with $L^2CS$, the base GCN is 1.2% inferior to GAT on average; after the data augmentation, $L^2CS$-GCN still falls behind $L^2CS$-GAT. However, compared with other baseline methods, $L^2CS$-GCN ranks second on Citeseer and Pubmed and third on Cora, exhibiting strong competitiveness. Please note that neither GCN nor GAT achieves outstanding accuracies compared with their strong counterparts: more concretely, even the original GAT cannot rank within the top three (with $L^2CS$-enhanced models excluded) on any dataset. This fact emphasizes the substantial effectiveness of $L^2CS$.

Figure 1: Overview of the $L^2CS$ pipeline. First, $L^2CS$ learns to cluster nodes within local regions, and aggregates the internal node features of the dense subgraph (i.e., cluster) to generate new nodes. Next, some original nodes in the training set can assign their labels to correspond generated nodes, and then $L^2CS$ predicts more unlabeled generated nodes through self-learning. Last, $L^2CS$ connects the generated nodes with the original nodes in the subgraph and augments the training set.
When calculating the specific accuracy enhancement brought by L²CS, we witness very significant 4.1% to 5.4% and 4.2% to 4.7% increases for GCN and GAT, respectively. Put these increments in the context: among all the other GCN-based approaches, the range of performance gain over GCN is -4.6% to 4.1%; among all the other GAT-based ones, it is -1.4% to 2.4% over GAT.

3.3 Ablation Analysis

In this section, we conduct some ablation analysis on the node attributes of the generated nodes, the label consistency within the updated subgraph, and the performance of each component.

To begin with, in Figure 2, we visualize original nodes and generated nodes with attributes as axes. While the former seem more crisscross, the latter exhibit clearer “community borders”, demonstrating that generated nodes have better class separability.

Next, to assess the label consistency within a dense subgraph, we design a straightforward experiment, which counts the percentage of dominating labels in each cluster partitioned by L²CS. We evaluate the original G and the updated G′ together and plot the occurrence densities of dominating label proportion in Figure 3. On all datasets tested, compared with the curves in G, those in G′ have higher peaks and are more right-gathered, implying that a larger proportion of nodes with subgraphs share the same labels.

Finally, we remove the components in L²CS and perform ablation experiments. The results are shown in Table 2. We find that the effect of overlapping clustering components can obviously achieve better results than non-overlapping ones. We think this is mainly due to the existence of mass fuzzy nodes in the graph, whose class separability of their attributes is weak (as shown in Figure 2). If such nodes are forced to belong to only a certain cluster, it is easy to introduce noise in the cluster or cause missing information in other clusters. In addition, as the augmented nodes exhibit higher quality and the added edges improve local label consistency, our data augmentation leads to higher performance gains.

4 CONCLUSION

In this paper, we propose a simple yet effective L²CS framework, which boosts the performance of graph-based SSL models by augmenting training resources. Aiming to strengthen the label similarity within dense subgraphs, L²CS generates high-quality nodes, which also exhibit refined class separability of attributes. Results of extensive evaluations indicate that this generic pre-processing technique can dramatically enhance the base algorithms and further outperform state-of-the-art baselines. Followup experiments and analyses present more insights regarding the superiority of L²CS. In the future, we will test L²CS in more setups, as well as explore other novel graph augmentation strategies.

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